

# ***“Decision Theory and Design in Multi-level hierarchical management structures”***

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# ***GENERAL THEME***

## ***CONTROL & DECISION MAKING PROBLEMS IN INTEGRATED OPERATIONS IN MANUFACTURING & FINANCE***

### ***ISSUES:***

- ▲ **INTEGRATED MANUFACTURING & HIERARCHICAL  
DECISION MAKING PROBLEMS**
- ▲ **FINANCE PROBLEMS & HIERARCHICAL DECISION MAKING**
- ▲ **NESTED DECISION & CONTROL PROBLEMS**

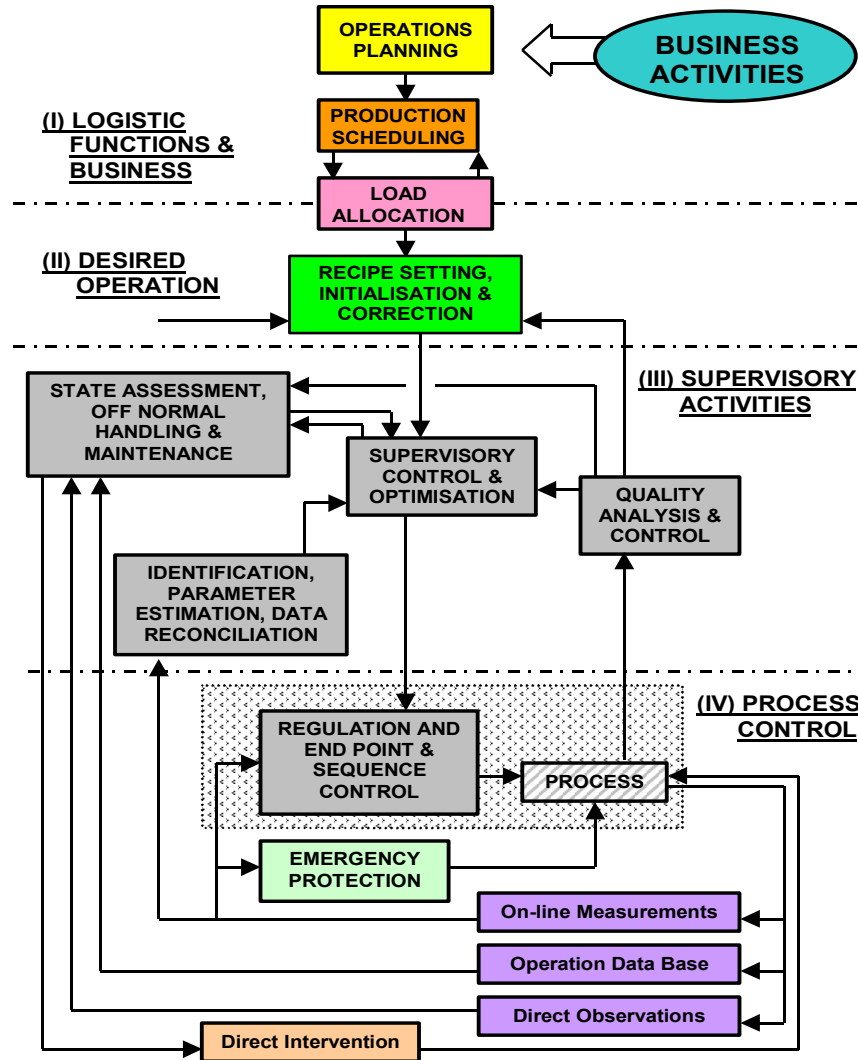


- ▲ **MULTI-LAYER CONTROL THEORY: GLOBAL  
CONTROLLABILITY & GLOBAL OBSERVABILITY**

# INTEGRATED PROCESS OPERATIONS

## Integrated System

**Systems Classification:**  
Discrete, Continuous,  
Mixed (Batch)



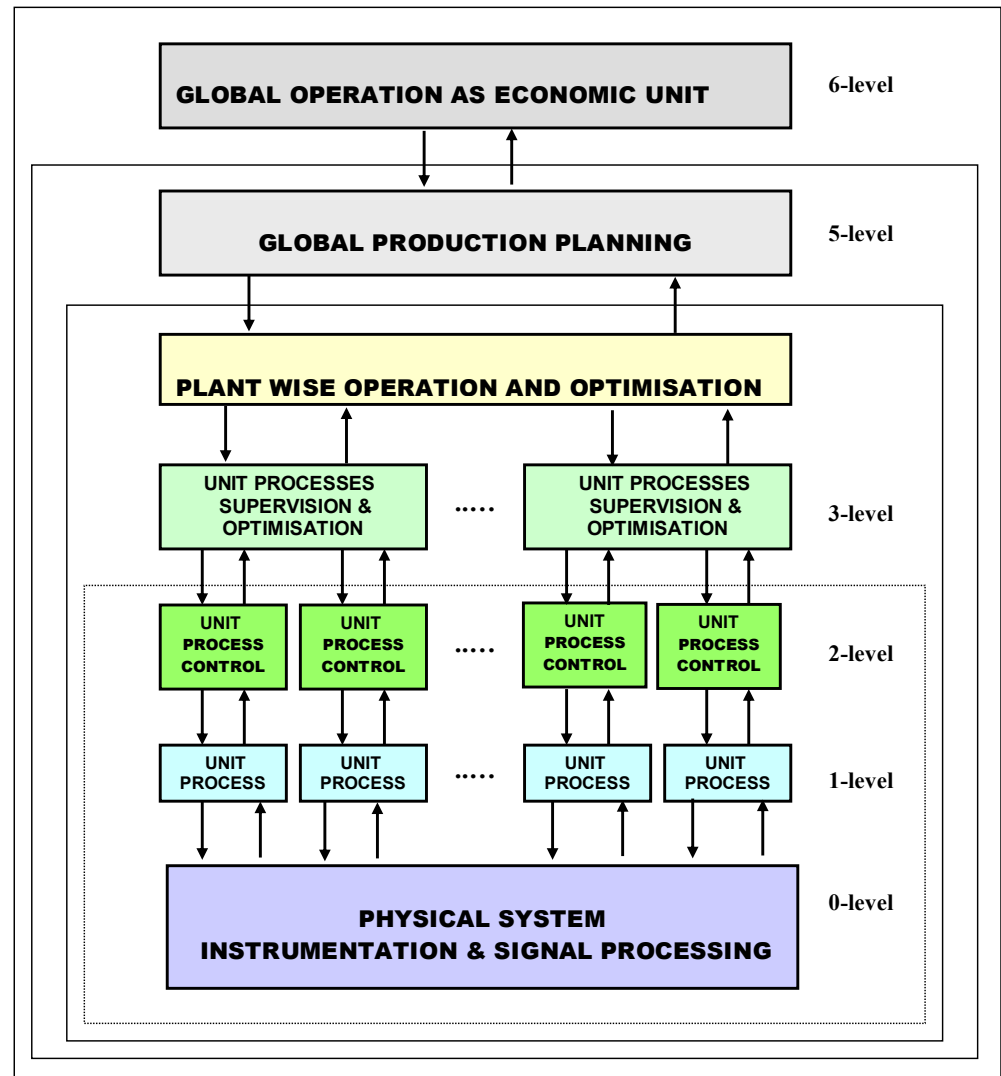
# SYSTEMS ORGANISATION

**PROBLEM:** ORGANISATION OF INFORMATION AND CONTROL-DECISION MAKING STRUCTURES

## CLASSIFICATION:

- HIERARCHICAL ORGANISATION
- HETERARCHICAL ORGANISATION
- HOLONIC ORGANISATION
- OTHERS (BIONIC, GENETIC, FRACTAL, RANDOM)

## HIERARCHICAL ORGANISATION

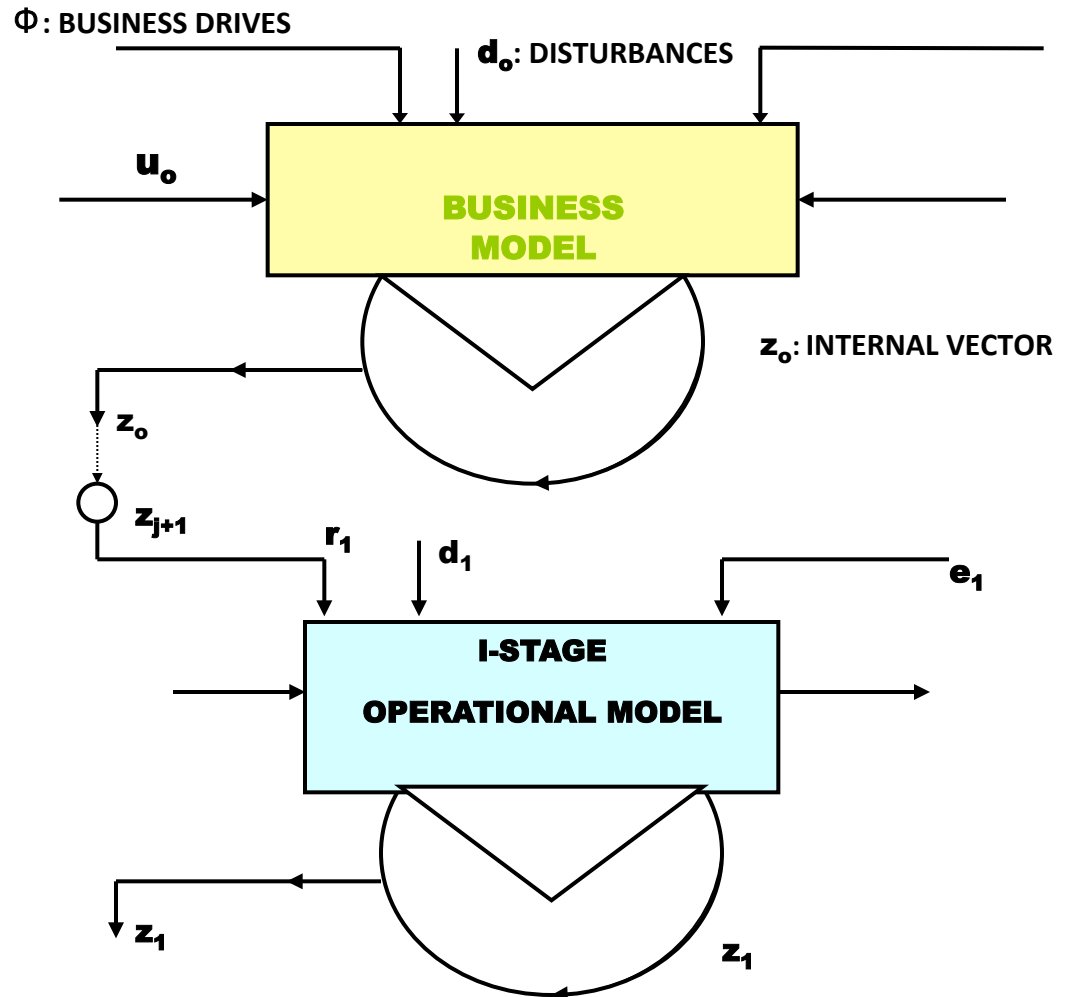


# CONTROL ARCHITECTURE IN A HIERARCHICAL ORGANISATION

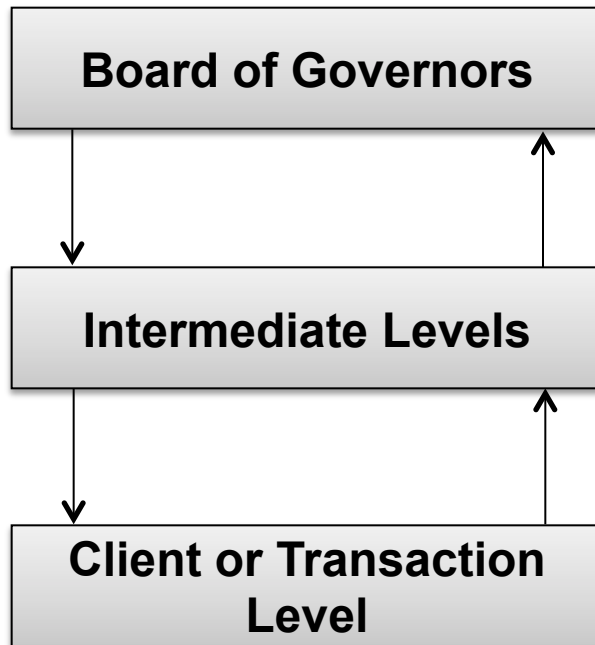
▲ Integration of Operations in Technological Processes:



- HYBRID SYSTEMS
- “TOP DOWN”: GLOBAL CONTROLLABILITY
- “BOTTOM UP”



# ***Multi-level Hierarchical Management System In Financial Institution***



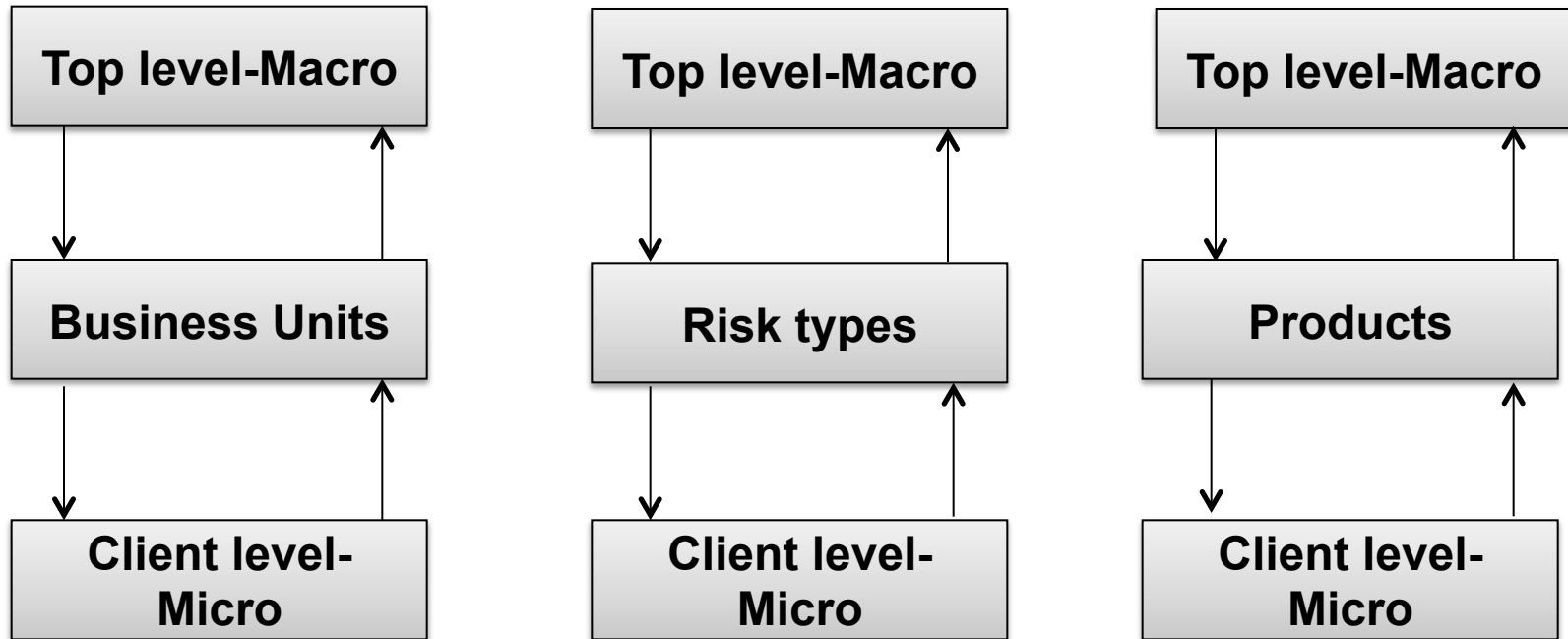
Macro

**Loan Management Problem**

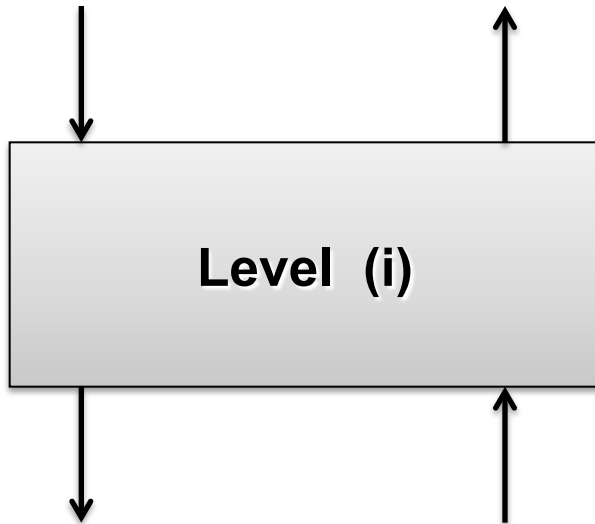
Micro

# *Intermediate Level Views*

## **Intermediate Levels have Different Views**



## ***Problem to be Solved in Every Level***



Maximise Profit

*Risk* < *d*



# ***Top-Down Approach***

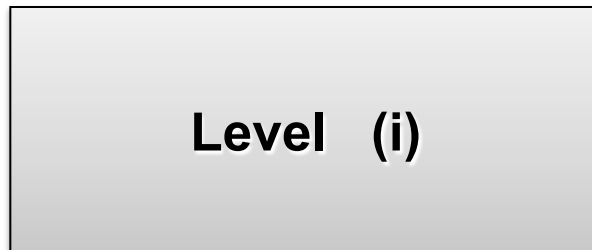
## **TASKS**

- 1) The Board sets the *profitability targets* and the *risk appetite* of the institution.**
- 2) This is translated to *profitability* and *risk appetite* to the lower levels.**
- 3) It is also translated to *credit risk policy* for *loan approval and management* at the lowest client level.**

# ***Main Tools for Credit Risk Management***

- **Rating Systems.**
- **Econometric Models for the calculation of *PD*, *LGD*, *EAD*.**
- **Database systems keeping the risk information for every client and transaction and being able to aggregate – disaggregate.**
- **Credit Management policies.**
- **Capital Management and allocation systems.**

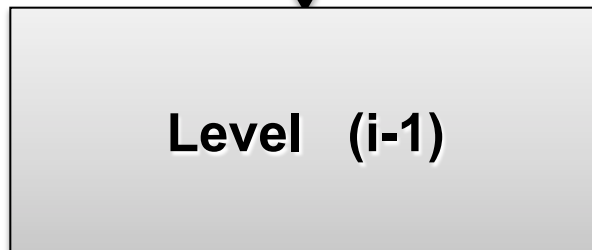
# ***Solution of the Optimisation Problems***



Maximise Profit

$$Risk < d$$

Optimal risk and pricing parameters



**Difference Equations of possible different sampling rates/scales**

Optimal risk and pricing parameters

# ***Models related to the problem***

**NOTE:** In every level, loans are observed in various states according to their repayment status and there is a state vector  $\underline{x}$  containing the total balance of loan at every state.

- ▲ The system describing the flows of loans between the various states is described by

$$\underline{x}_{n+1} = A \cdot \underline{x}_n + B \cdot \underline{u}_n$$

where  $\underline{u}_n$  is the vector of loans (approved). The output:  $\underline{y}_n = C \cdot \underline{x}_n$  describes the target values of risk and profit.

- ▲ The problem is then to maximise profit and keep risk in acceptable levels. We may also have other algebraic constraints, such as, liquidity, capacity and capital constraints.
- ▲ The optimal control problem can then be solved at each level using the solution of previous level as input to the next.
- ▲ The above system is related to the next level system by disaggregation and to the previous by aggregation.

# ***Outcome of the Optimisation Problem***

- ▲ **Top Level, risk appetite, capital levels for Credit Risk and optimal profit target**
- ▲ **Bottom Level, types of acceptable clients in terms of rating, exposure limits for every rating, exposure limits for every rating, collateral setting for every type of rating, pricing of loan.**
- ▲ **Intermediate Level, limits in average PD for every unit or product, limits of exposure for every unit or product. Profitability of every unit or product.**

# ***CONCLUSIONS***

- ▲ **Multilevel Hierarchically Nested Systems introduce the need for studying **Multilevel Hybrid Systems****
- ▲ **Multilevel Hybrid Systems require the introduction of notions of **Global Controllability** and **Global Observability**.**
- ▲ **The family of **Financial, Management Systems** is a paradigm of Multilevel Hybrid Systems**
- ▲ **Decisions are infiltrated from the top to the bottom level and results of actions are observed from the bottom to the top level**
- ▲ **An optimization problem can be defined by optimising profit keeping risk in acceptable levels**
- ▲ **This problem can be solved in stages starting from a macro level solution at the top and ending at an analytical or micro level at the bottom.**