

# Impact of regulatory standards on the eco-efficiency of firms

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# Motivation

- The internalisation of negative external effects is one of the most striking challenges in recent environmental research.
- One approach: Implementing environmental standards in the efficiency evaluation of firms.
- Eco-efficiency: We are looking for eco-efficient solutions such that the goods and services can be produced with less energy and resources and with less waste and emissions. (Heinz Felsner, see: Korhonen and Luptacik (2004))

⇒ We want to discuss the impact of regulatory constraints, in terms of environmental standards, on the eco-efficiency of firms measured with DEA.

## Relating Literature

- Basic literature:
  - Färe et al. (1989) and Shepard (1970): Introduced differentiation between strong and weak disposability.
  - Färe and Logan (1992): Using rate-of-return regulation, the authors were able to determine the relationship between measures of regulated and unregulated firms.
  - Golany and Roll (1994): Introduced the idea of implementing standards into the Data Envelopment Analysis (DEA) framework.
- Recent literature:
  - Korhonen and Luptacik (2004): Provided three different approaches for determining the eco-efficiency of firms.
  - Kuosmanen (2005): Formulation of weak disposability that allows for non-uniform abatement factors.
  - Yang and Pollitt (2010): Treated weakly and strongly disposable undesirable outputs.

# Environmental Standards

Limiting emissions while taking into account weak disposability of emissions.

- Intensity–regulation (Dudenhöffer (1984)):  $\frac{Emission}{Input} \leq \alpha_1$
- Emission per unit of output:  $\frac{Emission}{Output} \leq \alpha_2$
- Set level of emissions (limitation on absolute amount):  $Z \leq \alpha_3$

⇒ See Helfand (1991) and Luptacik (2009)

## Idea

- Environmental standards are introduced.
- Constraints on variables cannot be included in standard DEA framework, due to exogeneity.
- 2–step procedure:
  - ① Identifying polluting firms not fulfilling the environmental standard and creating standard–meeting projections.
  - ② Using DEA models for eco–efficiency on standard–meeting firms and projections.
- Difference in eco–efficiency scores between sample of regulated and unregulated firms as impact of the regulatory constraint for environmental standards.

## Step 1: Standard-meeting projections

- Weak disposability of emissions:
  - Reducing emissions by increasing inputs
  - Reducing emissions by reducing outputs
- Iterative processes programmed in Matlab detecting firms not meeting the environmental standard and creating projections with respect to weak disposability of emissions.
- Creating two samples:
  - 1 Unregulated firms: Original data
  - 2 Regulated firms: Standard-meeting firms and projections

## Step 2: Eco-efficiency Models

Korhonen and Luptacik (2004):

- Model A: Undesirable output (emissions) as negative output
- Model B: Undesirable output as input
- Model C: Undesirable output as input and input as negative output

⇒ Applying eco-efficiency models on the samples of regulated and unregulated firms.

⇒ Difference in eco-efficiency scores as impact of regulation.



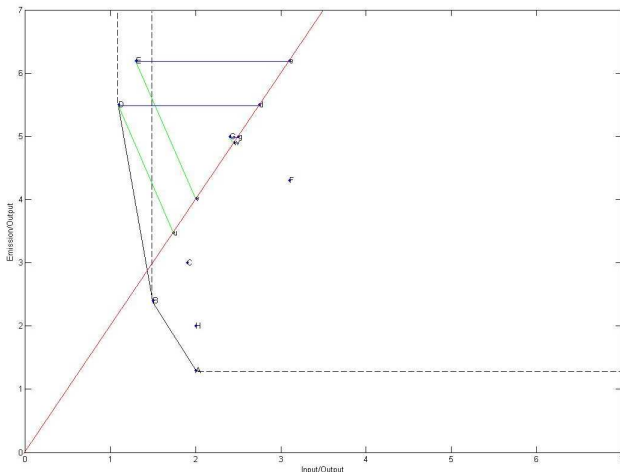
# Explanatory Example

- 8 Decision Making Units (DMU)
- 1 input, 1 desired output and 1 undesired output (emissions)
- Intensity regulation:  $\frac{Emission}{Input} \leq 2$

# DMU Data

	<b>Input</b>	<b>Emissions</b>	<b>Output</b>	$\frac{\text{Input}}{\text{Output}}$	$\frac{\text{Emission}}{\text{Output}}$	$\frac{\text{Emission}}{\text{Input}}$
<b>A</b>	20	13	10	2	1.3	0.7
<b>B</b>	15	24	10	1.5	2.4	1.6
<b>C</b>	19	30	10	1.9	3	1.6
<b>D</b>	11	55	10	1.1	5.5	5
<b>D1 (u)</b>	17.4	34.8	10	1.7	3.5	2
<b>D2 (d)</b>	11	22	4	2.8	5.5	2
<b>E</b>	13	62	10	1.3	6.2	4.8
<b>E1 (v)</b>	20.1	40.2	10	2	4	2
<b>E2 (e)</b>	13	26	4.2	3.1	6.2	2
<b>F</b>	31	43	10	3.1	4.3	1.4
<b>G</b>	24	50	10	2.4	5	2.1
<b>G1 (w)</b>	24.5	49	10	2.4	4.9	2
<b>G2 (g)</b>	24	48	9.6	2.5	5	2
<b>H</b>	20	20	10	2	2	1

# Graphical Presentation of Data



# Eco-efficiency scores and slacks using Model B

	Unregulated Firms			Regulated Firms				Regulatory Impact
	Score	Rank	Ref	Score	Slacks	Rank	Ref	
DMU A	1	1	A	1	0	1	A	
DMU B	1	1	B	1	0	1	B	
DMU C	0.79	6	A,B	0.79	0	5	A,B	
DMU D	1	1	D	0.86	6	4	B	0.14
DMU E	0.86	5	B,D	0.75	6	6	B	0.12
DMU F	0.51	8	A,B	0.51	0	8	A,B	
DMU G	0.59	7	B,D	0.61	6	7	B	-0.02
DMU H	0.89	4	A,B	0.89	0	3	A,B	
$\emptyset$ Efficiency	0.83			0.80				0.03

# Slack-Based-Measure (SBM) Models

- Slacks are included in efficiency scores
- Possible SBM models:
  - 1 Undesirable-output model
  - 2 Model B

# Slack-Based-Measure (SBM) Model for eco-efficiency (Model B)

$$\min_{\lambda, s^-, s^b} \rho = 1 - \frac{1}{m + s_2} \left( \sum_{i=1}^m \frac{s_i^-}{x_{io}} + \sum_{r=1}^{s_2} \frac{s_r^b}{y_{ro}^b} \right)$$

s.t.:

$$x_o = X\lambda + s^-$$

$$y_o^b = Y^b\lambda + s^b$$

$$y_o^g \leq Y^g\lambda$$

$$\lambda, s^-, s^b \geq 0$$

# Eco-efficiency scores using SBM of Model B

	Unregulated Firms			Regulated Firms			Regulatory Impact
	Score	Rank	Ref	Score	Rank	Ref	
<b>DMU A</b>	1	1	A	1	1	A	
<b>DMU B</b>	1	1	B	1	1	B	
<b>DMU C</b>	0.75	6	A,B	0.75	5	A,B	
<b>DMU D</b>	1	1	D	0.77	4	A,B	0.23
<b>DMU E</b>	0.82	5	B,D	0.66	6	A	0.16
<b>DMU F</b>	0.47	8	A	0.47	8	A	
<b>DMU G</b>	0.55	7	A	0.54	7	A	0.01
<b>DMU H</b>	0.83	4	A	0.83	3	A	
$\emptyset$ Efficiency	0.80			0.75			<b>0.05</b>

## Summary

- Internalising negative external effects by implementing environmental standards in benchmarking.
- Difference in eco-efficiency scores between sample of regulated and unregulated firms as regulatory impact of environmental standards.
- Could provide support for environmental policy makers in choosing appropriate instruments.
- Intensity of regulation could be assessed and adjusted.



# SBM Model B for eco-efficiency including bounded variables (Intensity Regulation)

$$\min_{\lambda, s^-, s^b} \rho = 1 - \frac{1}{m + s_2} \left( \sum_{i=1}^m \frac{s_i^-}{x_{io}} + \sum_{r=1}^{s_2} \frac{s_r^b}{y_{ro}^b} \right)$$

s.t.:

$$x_o = X\lambda + s^-$$

$$y_o = Y^b\lambda + s^b$$

$$y_o^g \leq Y^g\lambda$$

$$0 \leq Y^b\lambda \leq \alpha_1 X\lambda$$

$$\lambda, s^-, s^b \geq 0$$

## Eco-efficiency Results — SBM Model B bounded

	SBM Model B			SBM Model B bounded			Regulatory Impact
	Score	Rank	Ref	Score	Rank	Ref	
<b>DMU A</b>	1	1	A	1	1	A	
<b>DMU B</b>	1	1	B	1	1	B	
<b>DMU C</b>	0.75	6	A,B	0.75	4	$\tilde{D}$	
<b>DMU D</b>	1	1	D	0.70	6	$\tilde{D}$	0.3
<b>DMU E</b>	0.82	5	B,D	0.71	5	$\tilde{D}$	0.11
<b>DMU F</b>	0.47	8	A	0.47	8	A	
<b>DMU G</b>	0.55	7	A	0.55	7	A	
<b>DMU H</b>	0.83	4	A	0.83	3	A	
$\emptyset$ <b>Efficiency</b>	0.80			0.75			<b>0.05</b>

SBM Model B for eco-efficiency including bounded variables  
(emission per unit of output)

$$\min_{\lambda, s^-, s^b} \rho = 1 - \frac{1}{m + s_2} \left( \sum_{i=1}^m \frac{s_i^-}{x_{io}} + \sum_{r=1}^{s_2} \frac{s_r^b}{y_{ro}^b} \right)$$

s.t.:

$$x_o = X\lambda + s^-$$

$$y_o = Y^b\lambda + s^b$$

$$y_o^g \leq Y^g\lambda$$

$$0 \leq Y^b\lambda \leq \alpha_2 Y^g\lambda$$

$$\lambda, s^-, s^b \geq 0$$

SBM Model for eco-efficiency including bounded variables  
(level-of-emission)

$$\min_{\lambda, s^-, s^b} \rho = 1 - \frac{1}{m + s_2} \left( \sum_{i=1}^m \frac{s_i^-}{x_{io}} + \sum_{r=1}^{s_2} \frac{s_r^b}{y_{ro}^b} \right)$$

s.t.:

$$x_o = X\lambda + s^-$$

$$y_o^b = Y^b\lambda + s^b$$

$$y_o^g \leq Y^g\lambda$$

$$0 \leq Y^b\lambda \leq \alpha_3$$

$$\lambda, s^-, s^b \geq 0$$

# Possible additional constraints to account for weak disposability of undesirable outputs

- Constraints in radial DEA models (Yang and Pollitt (2010)):

$$\rho y_o^b = Y^b \lambda; \quad \rho y_o^g \leq Y^g \lambda$$

- Our first trial for SBM framework (Input increase):

$$\frac{(y_o^b - Y^b \lambda)}{y_o^b} = \frac{(X \lambda - x_o)}{x_o}$$

$$\frac{s^b}{y_o^b} = \frac{s_x^{WD}}{x_o}$$

- Our first trials for SBM framework (Output reduction):

$$\frac{(y_o^b - Y^b \lambda)}{y_o^b} = \frac{(y_o^g - Y^g \lambda)}{y_o^g}$$

$$\frac{s^b}{y_o^b} = \frac{s_y^{WD}}{y_o^g}$$

# SBM Model B for eco-efficiency including bounded variables and weak disposability (Intensity Regulation)

$$\min_{\lambda, s^-, s^b} \rho = 1 - \frac{1}{m + 2s_2} \left( \sum_{i=1}^m \frac{s_i^-}{x_{io}} + \sum_{r=1}^{s_2} \frac{s_r^b}{y_{ro}^b} + \sum_{i,r=1}^{s_2} \frac{s_r^{WD}}{x_{io}} \right)$$

s.t.:

$$x_o = X\lambda + s^-$$

$$y_o = Y^b\lambda + s^b$$

$$y_o^g \leq Y^g\lambda$$

$$0 \leq Y^b\lambda \leq \alpha_1 X\lambda$$

$$\frac{s_r^b}{y_{ro}^b} = \frac{s_r^{WD}}{x_{io}}$$

$$\lambda, s^-, s^b, s_r^{WD} \geq 0$$

# Undesirable-output model including bounded variables and weak disposability (Intensity Regulation)

$$\min_{\lambda, s^-, s^+} \rho = \frac{1 - \frac{1}{m} \sum_{i=1}^m \frac{s_i^-}{x_{io}}}{1 + \frac{1}{s_1 + 2s_2} \left( \sum_{r=1}^{s_1} \frac{s_r^g}{y_{ro}^g} + \sum_{r=1}^{s_2} \frac{s_r^b}{y_{ro}^b} + \sum_{r=1}^{s_2} \frac{s_r^{WD}}{y_{ro}^g} \right)}$$

s.t.:

$$x_o = X\lambda + s^-$$

$$y_o^b = Y^b\lambda + s^b$$

$$y_o^g = Y^g\lambda - s^g$$

$$0 \leq Y^b\lambda \leq \alpha_1 X\lambda$$

$$\frac{s_r^b}{y_{ro}^b} = \frac{s_r^{WD}}{y_{ro}^g}$$

$$\lambda, s^-, s^g, s^b, s_r^{WD} \geq 0$$

Thanks for your attention!



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